

ΑΣΚΗΣΗ 1 : (Reflected and Transmitted Powers)

(α) The refractive index of fused silica is calculated using the Sellmeier formula

$$n^2(\lambda) = 1 + \sum_{i=1}^3 \frac{B_i \lambda^2}{\lambda^2 - C_i}$$

where the freespace wavelength is expressed in microns.

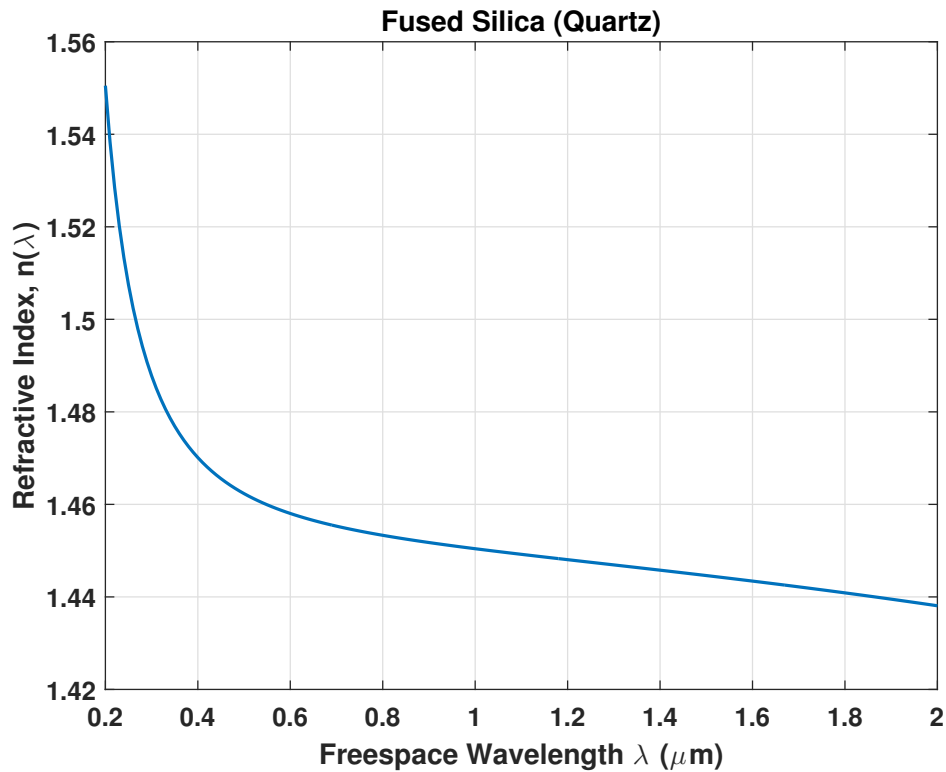
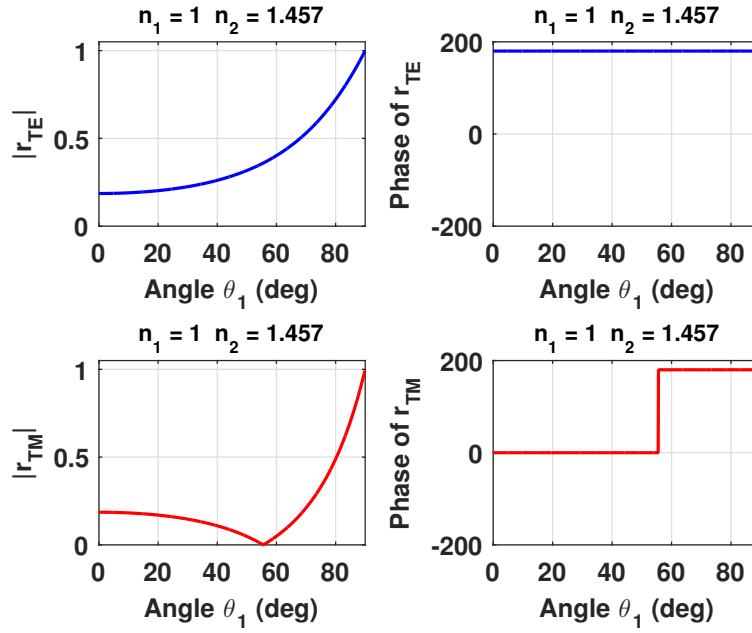
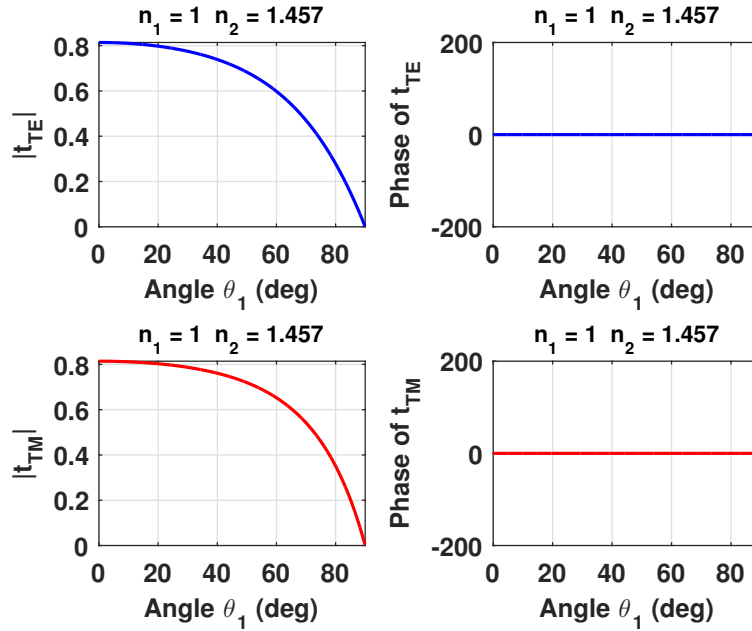


Figure 1: Fused silica (quartz) refractive index dependence on freespace wavelength.



(a)



(b)

Figure 2: (a) Reflection coefficients (TE and TM) as functions of the angle of incidence for $\lambda_0 = 0.633 \mu\text{m}$. (b) Transmission coefficients (TE and TM) as functions of the angle of incidence for $\lambda_0 = 0.633 \mu\text{m}$.

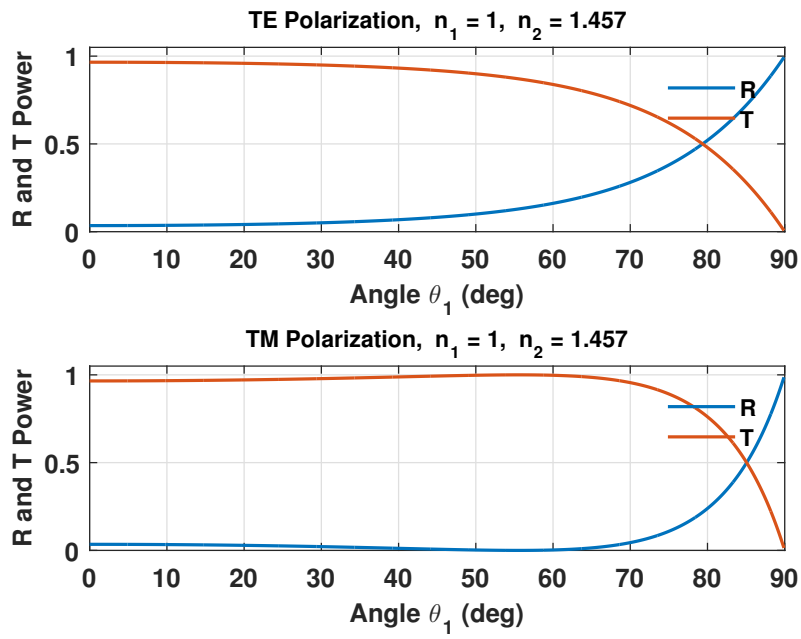
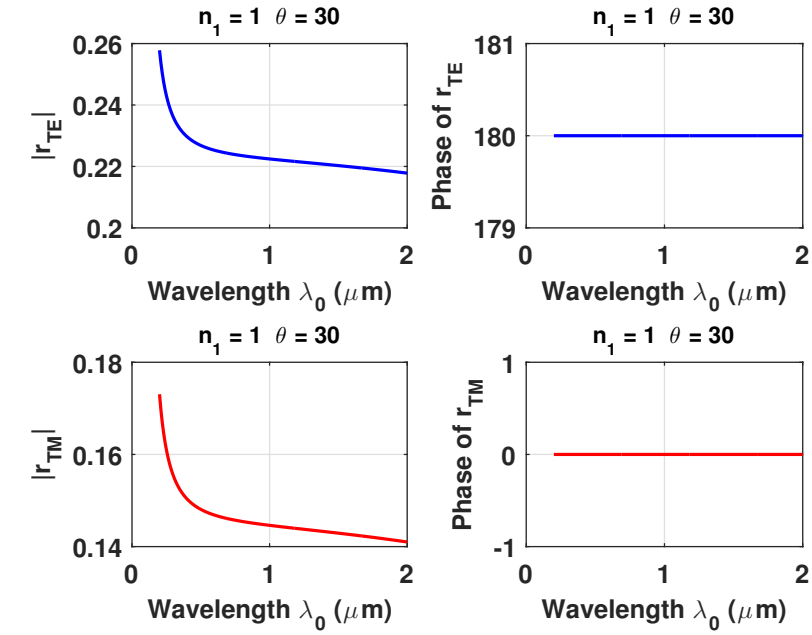
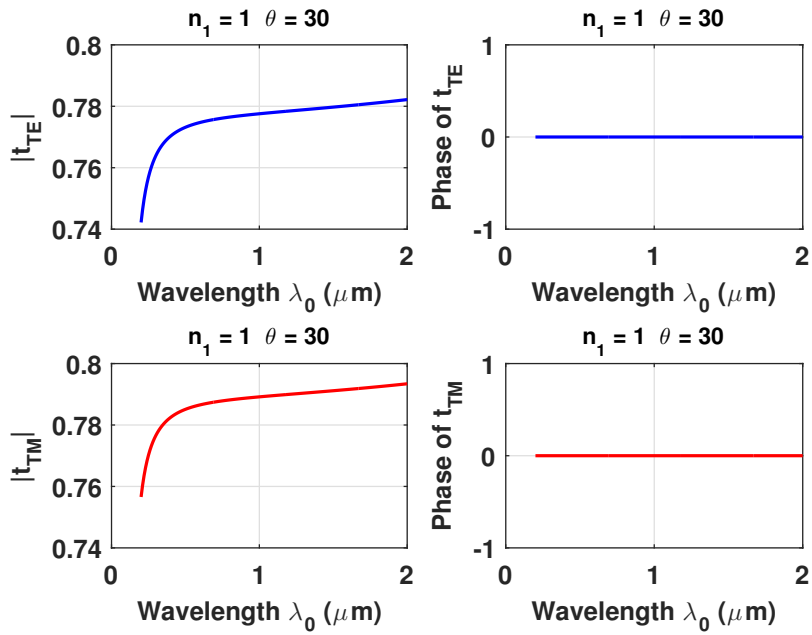


Figure 3: Reflected and transmitted powers (TE and TM) as functions of the angle of incidence for $\lambda_0 = 0.633 \mu\text{m}$.

(β)



(a)



(b)

Figure 4: (a) Reflection coefficients (TE and TM) as functions of the freespace wavelength for $\theta = 30$ deg. (b) Transmission coefficients (TE and TM) as functions of the freespace wavelength for $\theta = 30$ deg.

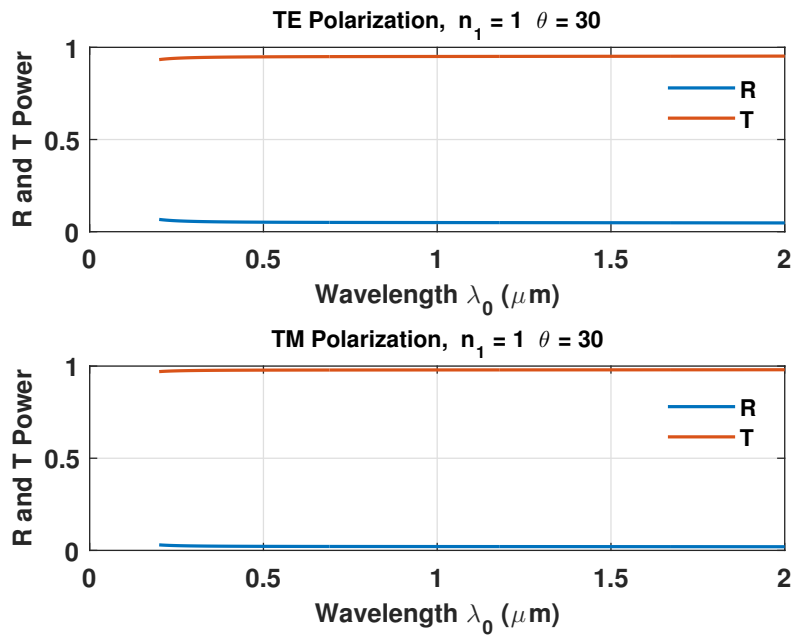
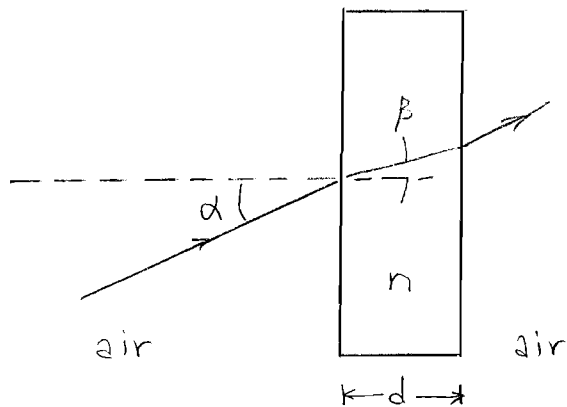


Figure 5: Reflected and transmitted powers (TE and TM) as functions of the freespace wavelength for $\theta = 30$ deg.

ΑΣΚΗΣΗ 2: (Interference Filter)



For maximum transmittance

$$2dn \cos \beta = m \lambda_0 \quad (1)$$

Filter is designed for λ_s
($\alpha = \beta = 0^\circ$)

$$2dn = m \lambda_s \quad (2)$$

From (1) & (2) we get:

$$m \lambda_s \cos \beta = m \lambda_0 \leadsto \lambda_0 = \lambda_s \cos \beta = \lambda_s \sqrt{1 - \sin^2 \beta} \Rightarrow$$

$$\Rightarrow \lambda_0 = \lambda_s \sqrt{1 - \frac{\sin^2 \alpha}{n^2}} \quad (3)$$

The angular tuning rate is defined as: $\frac{d\lambda_0}{d\alpha}$

$$\text{Therefore } \frac{d\lambda_0}{d\alpha} = \lambda_s \frac{1/2}{(1 - \sin^2 \alpha / n^2)^{1/2}} (-2 \sin \alpha \cos \alpha) \frac{1}{n^2} \Rightarrow$$

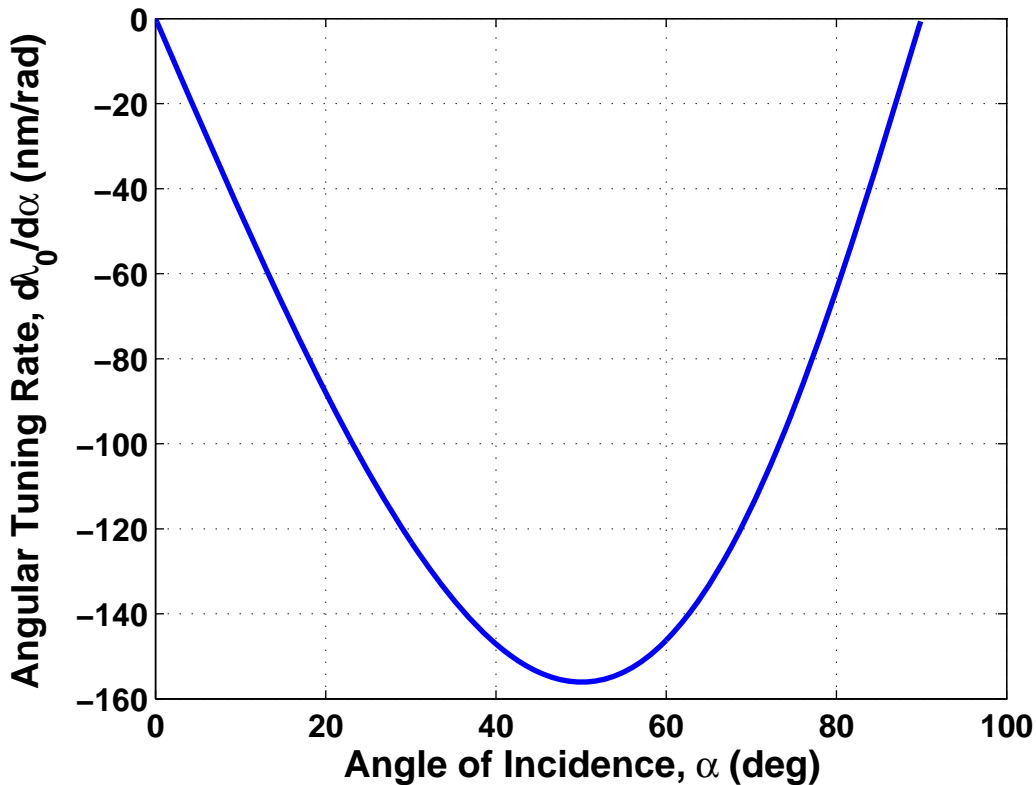
$$\frac{d\lambda_0}{d\alpha} = - \frac{\lambda_s \sin \alpha \cos \alpha}{n [n^2 - \sin^2 \alpha]^{1/2}} \quad (4)$$

For $\lambda_s = 520 \text{ nm}$ $\lambda_0 = 514.5 \text{ nm}$ and $n = 1.4$

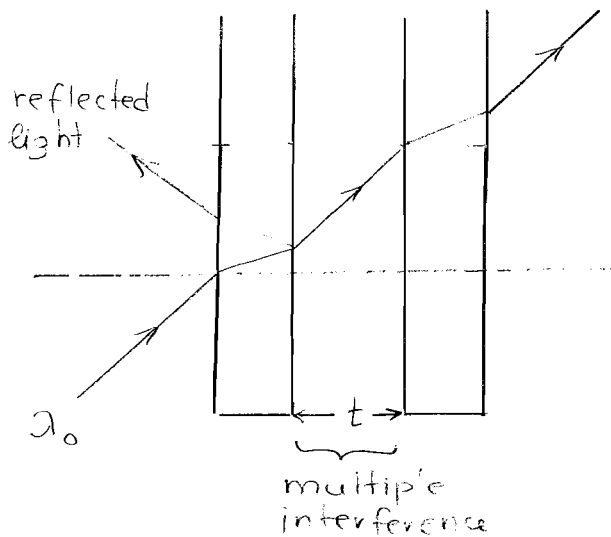
$$\text{From (3)} \leadsto \sin \alpha = n \left[1 - \left(\frac{\lambda_0}{\lambda_s} \right)^2 \right]^{1/2} \quad \alpha_0 = 11.71725^\circ$$

$$\left. \frac{d\lambda_0}{d\alpha} \right|_{\alpha_0} = - \frac{520 \text{ nm} \sin(\alpha_0) \cos(\alpha_0)}{1.4 [1.4^2 - \sin^2 \alpha_0]^{1/2}} = -53.32 \text{ nm/rad}$$

or $-0.9306 \text{ (nm/}^\circ)$



ΑΣΚΗΣΗ 3: (Fabry-Perot Filter)



We have multiple interference only between the surfaces separated by t . All other surfaces are considered slightly non parallel so the multiple interference from all other surfaces are neglected.

Resonance Conditions:

The dark lines in the reflected light correspond to minima in reflection or maxima on transmission.

$$2t n \cos \theta_t = m \lambda_0 \Rightarrow \lambda_0 = \frac{2t n \cos \theta_t}{m}$$

$$\theta_t = 45^\circ, t = 0.001 \text{ cm} = 10^{-3} \cdot 10^{-2} \text{ m} = 10^{-5} \text{ m} = 10^4 \text{ nm}$$

$$\text{For } 400 \text{ nm} < \lambda_0 < 700 \text{ nm} \sim$$

$$400 \text{ nm} < \frac{2 \cdot 10^4 \sqrt{2} / 2 \text{ nm}}{m} < 700 \text{ nm} \sim$$

$$400 < \frac{14142.135}{m} < 700 \sim$$

$$20.2 = \frac{14142.135}{700} < m < \frac{14142.135}{400} = 35.35$$

Therefore, the integer values of m are :

$$21, 22, \dots, 35.$$

As a result the dark lines are:

$$\lambda_0 = \frac{2t n \cos \theta_t}{m}$$

$$m = 21 \quad \rightarrow \quad \lambda_0 = 673.435 \text{ nm}$$

$$m = 22 \quad \rightarrow \quad \lambda_0 = 642.824 \text{ nm}$$

$$m = 23 \quad \rightarrow \quad \lambda_0 = 614.876 \text{ nm}$$

$$m = 24 \quad \rightarrow \quad \lambda_0 = 589.256 \text{ nm}$$

$$m = 25 \quad \rightarrow \quad \lambda_0 = 565.685 \text{ nm}$$

$$m = 26 \quad \rightarrow \quad \lambda_0 = 543.928 \text{ nm}$$

$$m = 27 \quad \rightarrow \quad \lambda_0 = 523.783 \text{ nm}$$

$$m = 28 \quad \rightarrow \quad \lambda_0 = 505.076 \text{ nm}$$

$$m = 29 \quad \rightarrow \quad \lambda_0 = 487.660 \text{ nm}$$

$$m = 30 \quad \rightarrow \quad \lambda_0 = 471.405 \text{ nm}$$

$$m = 31 \quad \rightarrow \quad \lambda_0 = 456.198 \text{ nm}$$

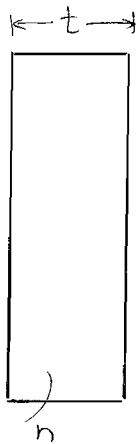
$$m = 32 \quad \rightarrow \quad \lambda_0 = 441.942 \text{ nm}$$

$$m = 33 \quad \rightarrow \quad \lambda_0 = 428.550 \text{ nm}$$

$$m = 34 \quad \rightarrow \quad \lambda_0 = 415.945 \text{ nm}$$

$$m = 35 \quad \rightarrow \quad \lambda_0 = 404.061 \text{ nm}$$

ΑΣΚΗΣΗ 4: (Fabry-Perot Filter)



$$n = 4.5, \quad t = 2 \text{ cm}$$

$$R = |r|^2 = 90\%$$

$$1 \text{ cm} = 10^{-2} \text{ m} = 10^7 \text{ nm}$$

$$\lambda_0 \approx 546 \text{ nm}$$

(a) Maximum transmission: $2tn \cos \theta_t = m \lambda_0$

Maximum m occurs for $\theta_t = 0^\circ \Rightarrow m \lambda_0 = 2tn \Rightarrow$

$$m = \left[\frac{2tn}{\lambda_0} \right] = \left[\frac{2 \cdot 2 \cdot 10^7 \text{ nm} \cdot 4.5}{546 \text{ nm}} \right] = [329670.33]$$

$$= 329670$$

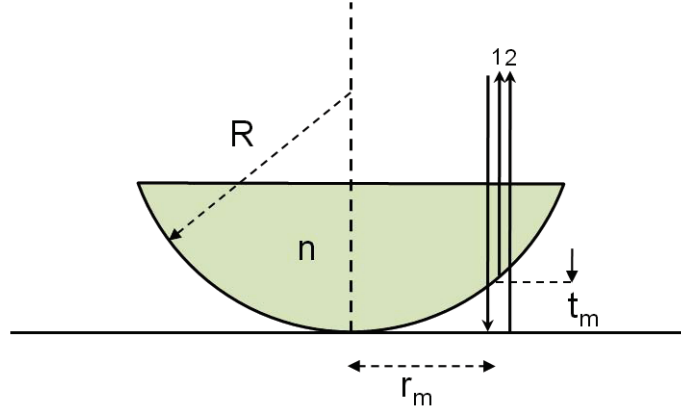
(β) $\frac{T_{\max}}{T_{\min}} = \frac{1}{1/(1+F)} = 1+F$

$$F = \frac{4r^2}{(1-r^2)^2} = 360$$

$$\left. \begin{array}{l} \frac{T_{\max}}{T_{\min}} = 1+F \\ F = 360 \end{array} \right\} \Rightarrow \frac{T_{\max}}{T_{\min}} = 361$$

(c) $\mathcal{R} \approx \frac{\pi}{2} m \sqrt{F} = \frac{\pi}{2} 329670 \sqrt{360} = 9.825 \cdot 10^6$

ΑΣΚΗΣΗ 5 : (Newton's Rings)



The interference rings are formed from interference between waves that reflect at the inner surface of the spherical interface (like ray 1 shown in the figure) and at the optically flat bottom surface (like ray 2 shown in the figure). In order to get constructive interference the following condition should be satisfied:

$$2n_{air}t_m + \Delta_{refl} = m\lambda_0,$$

where $\Delta_{refl} = \lambda_0/2$ since ray 1 experiences an internal reflection while ray 2 experiences an external reflection. Therefore, the constructive interference condition becomes

$$2n_{air}t_m = (2m + 1)\frac{\lambda_0}{2}, \quad m = 0, 1, \dots$$

The tenth bright ring corresponds to $m = 9$. For $n_{air} = 1$ then $2t_9 = 19(\lambda_0/2)$. The relation between t_m and r_m is given by

$$r_m^2 + (R - t_m)^2 = R^2 \implies r_m = \sqrt{2Rt_m - t_m^2},$$

Then for $\lambda_0 = 546.1 \text{ nm}$ the value of $t_9 = (19/2)(\lambda_0/2) = 2593.975 \text{ nm} = 2.593975 \times 10^{-6} \text{ m}$ and $r_9 = 7.89/2 = 3.945 \text{ mm}$ solving for R the previous equation it can be found that

$$R = \frac{r_m^2 + t_m^2}{2t_m} = \frac{r_9^2 + t_9^2}{2t_9} = \frac{3.945^2 \times 10^{-6} + 2.593975^2 \times 10^{-12}}{2 \times 2.593975 \times 10^{-6}} \text{ m} = 2.9998 \text{ m} \simeq 3 \text{ m}.$$

The focal distance can be found from the equation

$$\frac{1}{f} = (n - 1)\left(\frac{1}{R_1} - \frac{1}{R_2}\right) = (1.5 - 1)\left(\frac{1}{\infty} - \frac{1}{-3 \text{ m}}\right) \implies f \simeq 6 \text{ m}$$