

Θεμα 1

(α)

$$\Phi(z) = \frac{\lambda a}{2\epsilon_0} \left[ \frac{1}{[(z-h)^2 + a^2]^{1/2}} - \frac{1}{[(z+h)^2 + a^2]^{1/2}} \right] \quad (z \geq 0)$$

$$\Phi(z) = 0 \quad (z \leq 0)$$

(β)

$$\vec{E} = \hat{i}_z \frac{\lambda a}{2\epsilon_0} \left[ \frac{z-h}{[(z-h)^2 + a^2]^{3/2}} - \frac{z+h}{[(z+h)^2 + a^2]^{3/2}} \right] \quad (z \geq 0)$$

$$\vec{E} = 0 \quad (z \leq 0)$$

(γ)

$$\sigma(0, 0, 0) = -\lambda a \frac{h}{(h^2 + a^2)^{3/2}}$$

(δ)

$$\Phi(x, y, z) = \Phi_+(x, y, z) + \Phi_-(x, y, z) \quad (z \geq 0)$$

$$\Phi_+(x, y, z) = +\frac{\lambda a}{4\pi\epsilon_0} \int_0^{2\pi} \frac{d\phi}{[(x - a \cos \phi)^2 + (y - a \sin \phi)^2 + (z - h)^2]^{1/2}}$$

$$\Phi_-(x, y, z) = -\frac{\lambda a}{4\pi\epsilon_0} \int_0^{2\pi} \frac{d\phi}{[(x - a \cos \phi)^2 + (y - a \sin \phi)^2 + (z + h)^2]^{1/2}}$$

$$\Phi(x, y, z) = 0 \quad (z \leq 0)$$

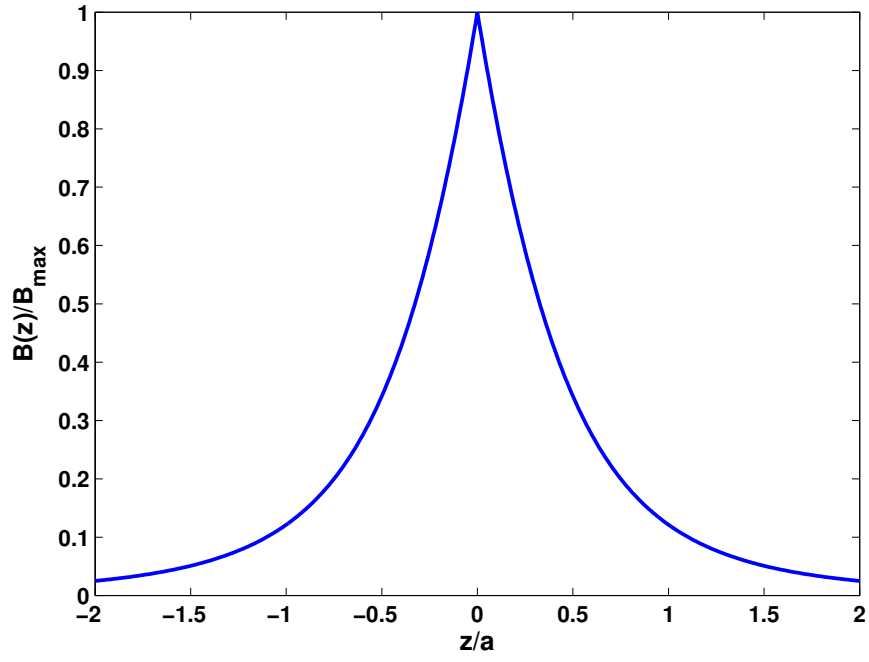
Θεμα 2

(α)

$$\vec{B} = \hat{i}_z \frac{\mu_0 K_0}{2} \left[ \frac{a^2 + 2z^2}{(a^2 + z^2)^{1/2}} - 2|z| \right]$$

(β)

$$B_{max} = B(z=0) = \hat{i}_z \frac{\mu_0 K_0 a}{2}$$



( $\gamma$ )

$$\vec{A} = \frac{\mu_0}{4\pi} \int_{r'_T=0}^a \int_{\phi'=0}^{2\pi} \frac{K_0[-\sin\phi'\hat{i}_x + \cos\phi'\hat{i}_y]r_T'^2 dr'_T d\phi'}{[r^2 + r_T'^2 - 2rr_T' \sin\theta \cos(\phi - \phi')]^{1/2}}$$

( $\delta$ )

$$\vec{A}(r, \theta = 0, \phi) = 0$$

$\Theta\epsilon\mu\alpha$  3 $(\alpha)$ 

$$\Phi(x, y) = \begin{cases} V_0 \cos(ky) e^{kx} & -\infty < x \leq 0 \text{ and } \forall y, \\ -V_0 \cos(ky) \frac{\sinh[k(x-d)]}{\sinh(kd)} & 0 \leq x \leq d \text{ and } \forall y, \\ 0 & d \leq x < +\infty \text{ and } \forall y. \end{cases}$$

 $(\beta)$ 

$$\vec{E}(x, y) = \begin{cases} kV_0 e^{kx} [-\cos(ky)\hat{i}_x + \sin(ky)\hat{i}_y] & -\infty < x \leq 0 \text{ and } \forall y, \\ kV_0 \left[ \cos(ky) \frac{\cosh[k(x-d)]}{\sinh(kd)} \hat{i}_x - \sin(ky) \frac{\sinh[k(x-d)]}{\sinh(kd)} \hat{i}_y \right] & 0 \leq x \leq d \text{ and } \forall y, \\ 0 & d \leq x < +\infty \text{ and } \forall y. \end{cases}$$

 $(\gamma)$ 

$$\sigma(x=0, y) = \epsilon k V_0 \cos(ky) \frac{\cosh(kd)}{\sinh(kd)} + \epsilon_0 k V_0 \cos(ky)$$

$$\sigma(x=d, y) = -\epsilon k V_0 \cos(ky) \frac{1}{\sinh(kd)}$$

 $\Theta\epsilon\mu\alpha$  4 $(\alpha)$ 

$$\Phi(r_T) = -V \frac{\ln(r_T/b)}{\ln(b/a)}$$

$$\vec{E} = \frac{V}{\ln(b/a)} \frac{1}{r_T} \hat{i}_{r_T}$$

 $(\beta)$ 

$$\frac{C}{\ell} = \frac{\pi(\epsilon + \epsilon_0)}{\ln(b/a)}$$