

Θεμα 1

(α)

$$\vec{E} = \begin{cases} \left[ \frac{\rho_0}{2\epsilon_0} x_0 + \frac{\lambda_0}{2\pi\epsilon_0} (x - x_0) \right] \hat{i}_x + \left[ \frac{\rho_0}{2\epsilon_0} y_0 + \frac{\lambda_0}{2\pi\epsilon_0} (y - y_0) \right] \hat{i}_y & \text{for } r_{T1} < a, \\ & \text{and } r_{T2} < b, \\ \left[ \frac{\rho_0}{2\epsilon_0} x + \frac{\lambda_0 - b^2 \pi \rho_0}{2\pi\epsilon_0} \frac{x - x_0}{(x - x_0)^2 + (y - y_0)^2} \right] \hat{i}_x + \left[ \frac{\rho_0}{2\epsilon_0} y + \frac{\lambda_0 - b^2 \pi \rho_0}{2\pi\epsilon_0} \frac{y - y_0}{(x - x_0)^2 + (y - y_0)^2} \right] \hat{i}_y & \text{for } r_{T1} < a, \\ & \text{and } r_{T2} > b, \\ \left[ \frac{\rho_0}{2\epsilon_0} \frac{x}{x^2 + y^2} + \frac{\lambda_0 - b^2 \pi \rho_0}{2\pi\epsilon_0} \frac{x - x_0}{(x - x_0)^2 + (y - y_0)^2} \right] \hat{i}_x + \left[ \frac{\rho_0}{2\epsilon_0} \frac{y}{x^2 + y^2} + \frac{\lambda_0 - b^2 \pi \rho_0}{2\pi\epsilon_0} \frac{y - y_0}{(x - x_0)^2 + (y - y_0)^2} \right] \hat{i}_y & \text{for } r_{T1} > a, \\ r_{T1} = [x^2 + y^2]^{1/2} \quad r_{T2} = [(x - x_0)^2 + (y - y_0)^2]^{1/2}. \end{cases}$$

(β)

$$\frac{k - 1}{k} = \frac{b^2 \rho \pi - \lambda_0}{a^2 \pi \rho_0}$$

(γ)

$$\vec{f} = \frac{\lambda_0 \rho_0}{2\epsilon_0} [x \hat{i}_x + y \hat{i}_y]$$

Θεμα 2

(α)

$$\vec{H} = \begin{cases} \left[ -\frac{I_1}{2\pi} \frac{y}{x^2 + y^2} + \frac{K_2}{2} \right] \hat{i}_x + \left[ \frac{I_1}{2\pi} \frac{x}{x^2 + y^2} \right] \hat{i}_y & \text{for } z > -y \tan \theta, \\ \left[ -\frac{I_1}{2\pi} \frac{y}{x^2 + y^2} - \frac{K_2}{2} \right] \hat{i}_x + \left[ \frac{I_1}{2\pi} \frac{x}{x^2 + y^2} \right] \hat{i}_y & \text{for } z < -y \tan \theta. \end{cases}$$

(β)

$$\vec{f} = \frac{I_1}{2\pi} \mu_0 \left[ K_2 \sin \theta \frac{x}{x^2 + y^2} \hat{i}_x - K_2 \sin \theta \frac{y}{x^2 + y^2} \hat{i}_y + K_2 \cos \theta \frac{y}{x^2 + y^2} \hat{i}_z \right]_{z = -y \tan \theta}$$

(γ)

$$\vec{f} = \begin{cases} \frac{\mu_0 I_1 K_2}{2} \hat{i}_y & \text{for } z > 0, \\ \frac{\mu_0 I_1 K_2}{2} \hat{i}_y & \text{for } z < 0. \end{cases}$$

(δ)

Cylinder

$$x^2 + \left( y - \frac{I_1}{2\pi K_2} \right)^2 = \left( \frac{I_1}{2\pi K_2} \right)^2 \quad \text{and } z > -y \tan \theta$$

Cylinder

$$x^2 + \left(y + \frac{I_1}{2\pi K_2}\right)^2 = \left(\frac{I_1}{2\pi K_2}\right)^2 \quad \text{and } z < -y \tan \theta$$

$\Theta\epsilon\mu\alpha$  3

( $\alpha$ )

$$\beta = \omega\sqrt{\epsilon_0\mu_0}, \quad \text{Righthanded Elliptical Polarization}$$

( $\beta$ )

$$\vec{E}_r = E_0[-2 \hat{i}_x + j \hat{i}_y] \exp[+j\beta z]$$

Lefthanded Elliptical Polarization

$$\vec{H}_r = \frac{E_0}{Z_0}[j \hat{i}_x + 2 \hat{i}_y] \exp[+j\beta z]$$

( $\gamma$ )

$$\vec{\mathcal{E}}(z, t) = E_0 \sin(\beta z)[4 \sin(\omega t) \hat{i}_x - 2 \cos(\omega t) \hat{i}_y]$$

( $\delta$ )

$$\sigma(t) = 0,$$

$$\vec{\mathcal{K}}(t) = \frac{2E_0}{Z_0}[2 \cos(\omega t) \hat{i}_x + \sin(\omega t) \hat{i}_y].$$

( $\epsilon$ )

$$\vec{f} = \frac{\mu_0}{2} \left(\frac{2E_0}{Z_0}\right)^2 [\cos^2(\omega t) + 1] \hat{i}_z$$
$$\langle \vec{f} \rangle = \frac{3\mu_0}{4} \left(\frac{2E_0}{Z_0}\right)^2 \hat{i}_z$$