# Parametric investigation of rigid blocks subjected to synthetic near-source ground motions



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## introduction

we perform a systematic investigation of the seismic response of rigid blocks subjected to near-source records of different magnitudes

and high frequency component for a dip-slip fault

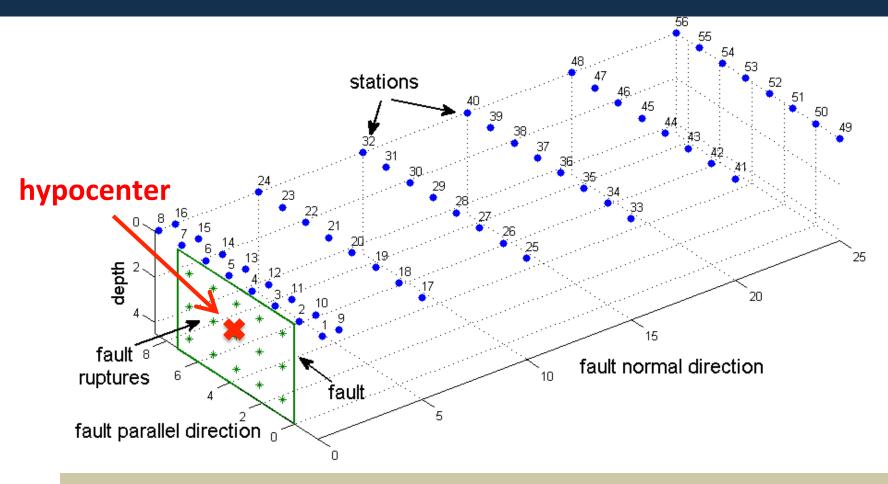
generate synthetic pulse-like

ground-motions consisting of a **low** 

consider several rigid block structures of **different geometry** 

parametric investigation that improves our understanding on the effect of base motion characteristics on the overturning rigid block structures

## synthetic ground motions



- assume a vertical fault and a grid of 56 receiver stations
- consider events with  $M_w$  =5.5, 6.0, 6.5, 7.0 and 7.5 the fault size varies accordingly
- simulate 100 fault ruptures recorded at the 56 receiver stations

## synthetic ground motions

**The low frequency** component is defined by means of a wavelet of the form:

$$V(t) = 0.5 A_{p} \left[ + \cos \left( \frac{2\pi f_{p}}{\gamma_{p}} (t - t_{0}) \right) \right] \cos \left[ 2\pi f_{p} (t - t_{0}) + v_{p} \right]$$

this is a **four-parameter** wavelet whose parameters are randomly sampled:

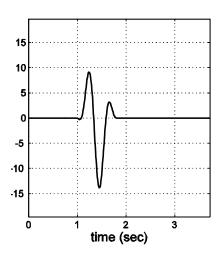
•  $A_p$ : amplitude of the velocity pulse  $A_p$ =0.9 PGV:

$$\log PGV = 2.040 - 0.032r_{rup}$$

•  $f_p$ : pulse frequency:

$$\log T_{\rm p} = -2.9 + 0.5 M_{\rm W}$$

- $v_p$ : the phase angle, normally distributed
  - $y_p$ : the number of cycles, normally distributed



## rigid block structures

Following the work of Housner (1963), the equation of motion of a rocking rigid block is:

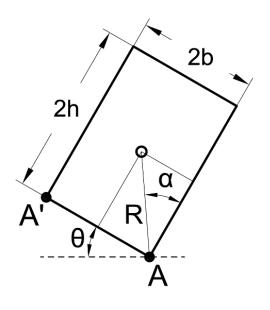
$$\ddot{\theta}(t) = p^{2} \left[ -\alpha \operatorname{sgn}(\theta(t)) + \theta(t) - \ddot{u}_{g}(t) / g \right]$$

the geometry of the block is fully described by the slenderness angle  $\alpha$ :

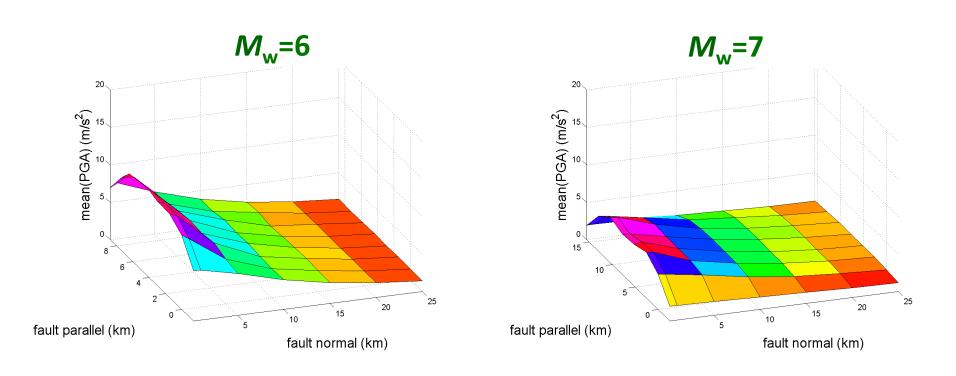
$$\alpha = \operatorname{atan}(b/h)$$

and the frequency parameter p:

$$p = \sqrt{\frac{WR}{I_0}} = \sqrt{\frac{3g}{4R}}$$



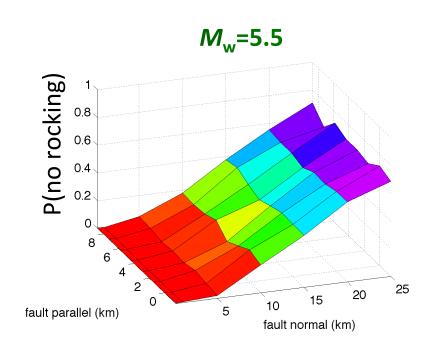
## peak ground acceleration

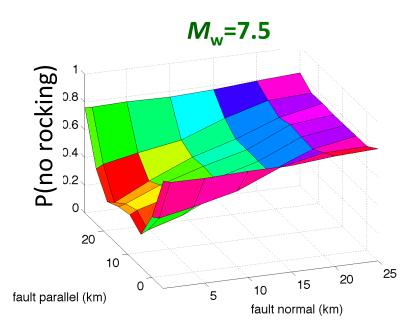


#### Distribution of the mean peak ground accelerations (PGA):

- larger PGAs close to the epicenter (as expected)
- events of smaller magnitude M<sub>w</sub> produce larger PGAs

## no rocking initiation

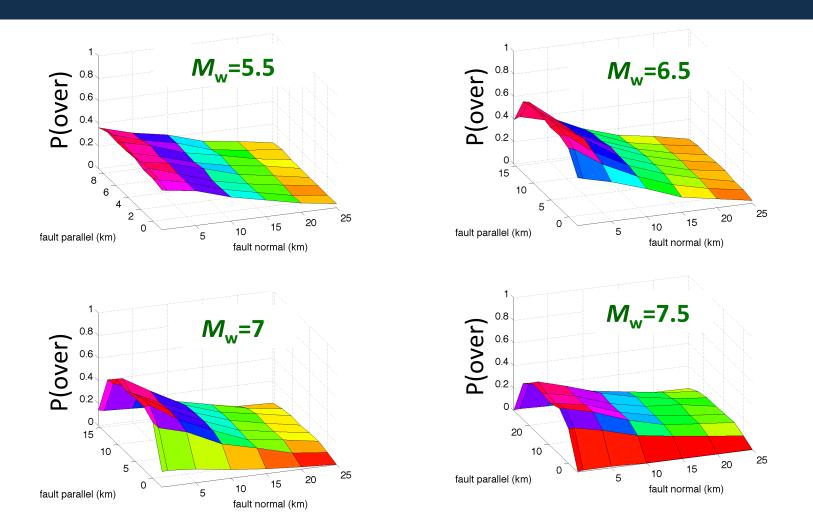




rocking is initiated only if **PGA/g** tan $\alpha \ge 1$ , thus:

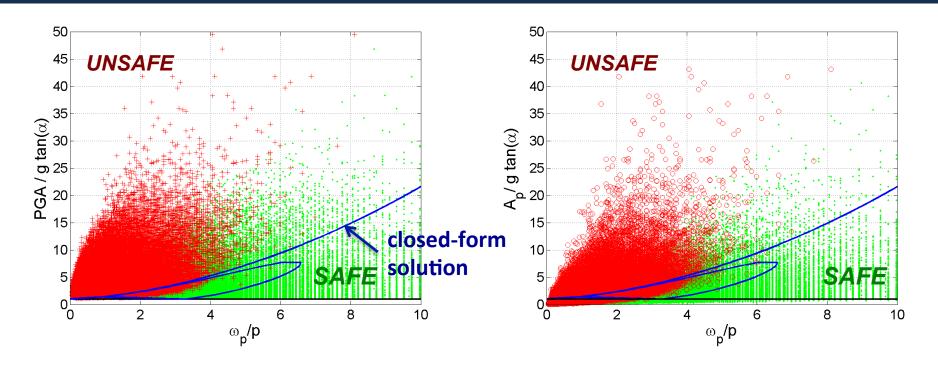
- for  $M_w$ =5.5 all ground motions set the blocks to motion, but this is not the case for the  $M_w$ =7.5 events
- at large distances, most probably, the block will remain at rest

## overturning probability



Overturning probabilities do not follow the trend of PGAs, i.e. small values for  $M_{\rm w}$ =5.5, maximum for  $M_{\rm w}$ =6.5 and decrease again for  $M_{\rm w}$  > 7.0

## overturning spectra

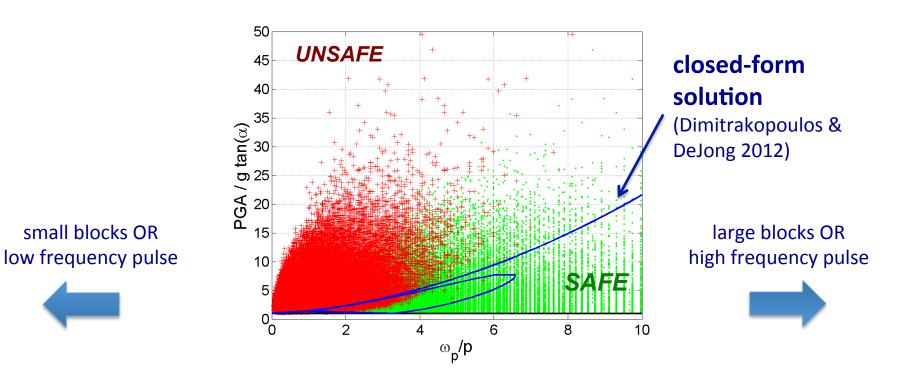


we present results in the form of overturning spectra: i.e. graphs of frequency  $\omega_p/p$  versus amplitude PGA/gtan $\alpha$  or  $A_p/gtan\alpha$ 

#### PGA/(g tan $\alpha$ ) is preferable over $A_p$ /(g tan $\alpha$ ):

- easier to calculate
- respects the condition that rocking will immense only if PGA/(g tan $\alpha$ )  $\geq 1$ .

## overturning spectra

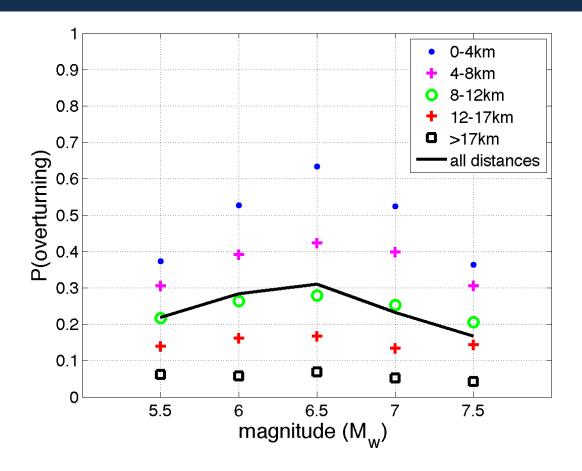


many blocks on the "unsafe" region do not overturn

small blocks OR

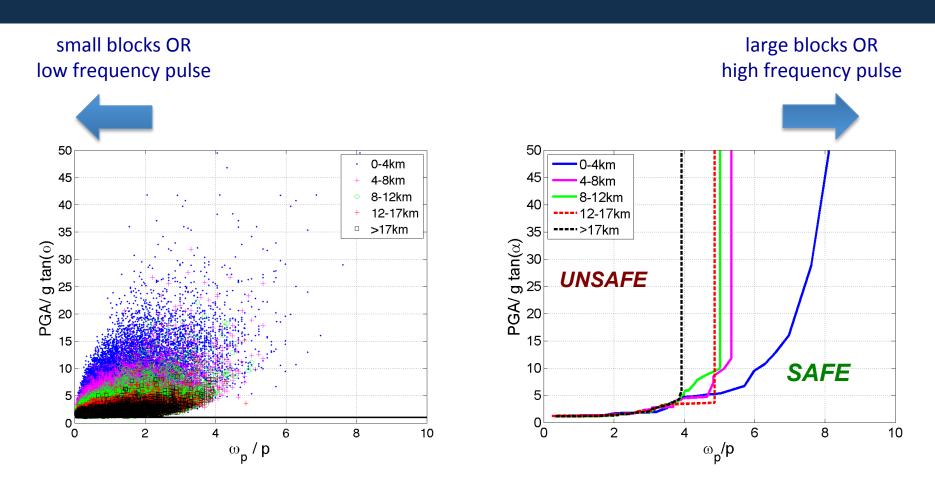
- For large  $\omega_p$ /p values overturning is rather improbable, especially for  $\underline{\omega}_p/p \ge 8$  (regardless of the PGA)
- sinusoidal pulses are overall more conservative, especially for  $\omega_p/p \ge 6$ .

## effect of distance



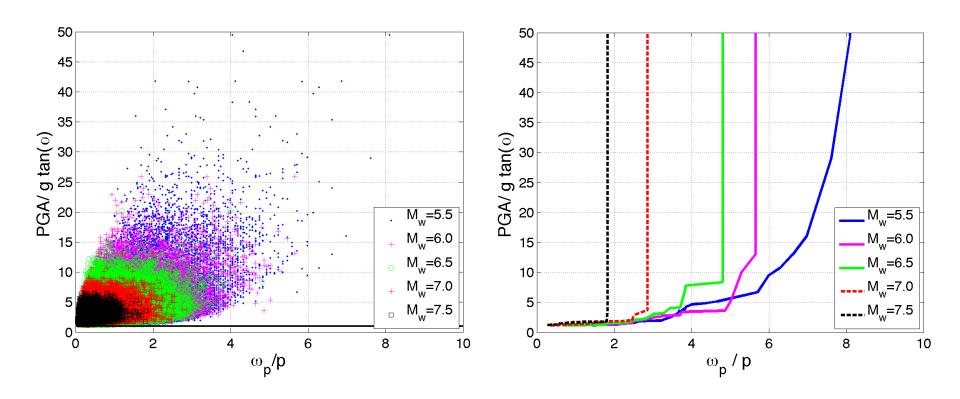
- Very high overturning probabilities close to the fault and very small as we move away
- Magnitude 6.5 is the most critical (compare to  $M_w$ =5.5 and  $M_w$ =7.5)

## effect of distance



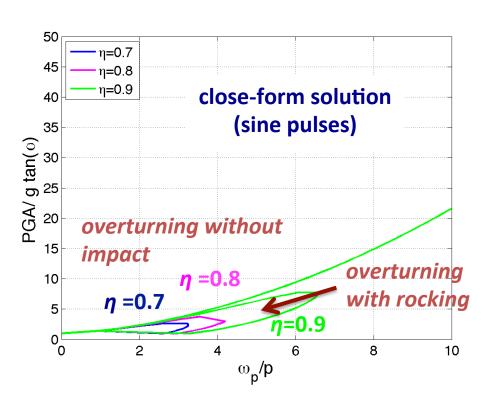
- the number of blocks that overturn decrease with distance
- distance seems important only when  $\omega_p/p \ge 4$

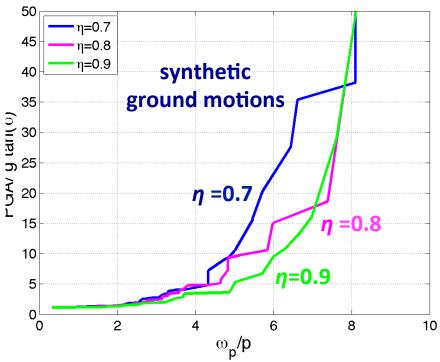
## effect of magnitude



- distinct differences looking at different M<sub>w</sub> events (threshold curves)
- for a given block, p value -> only small values of  $\omega_p/p$  can be attained for large  $M_w$ , hence the threshold curves move to the left as  $M_w$  increases
- for large  $M_w$  the blocks overturn for a small PGA/g tan $\alpha$ , thus for large  $M_w$  if rocking initiates, the block will most probably overturn

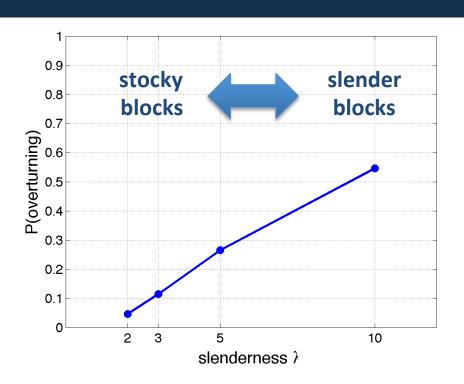
### coefficient of reinstitution

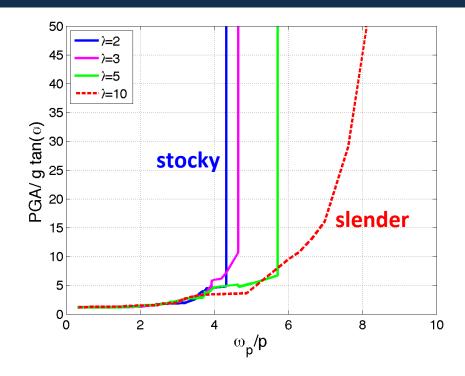




- closed-form solutions from sine pulses  $\rightarrow \eta$  is of some minor importance when overturning with rocking occurs
- when synthetic records are considered, small effect on the overturning probability for  $\eta = 0.8$  and  $\eta = 0.9$ , some sensitivity for  $\eta = 0.7$ .
- In all, we don't need to "exactly" know the value of  $\eta$

## block slenderness

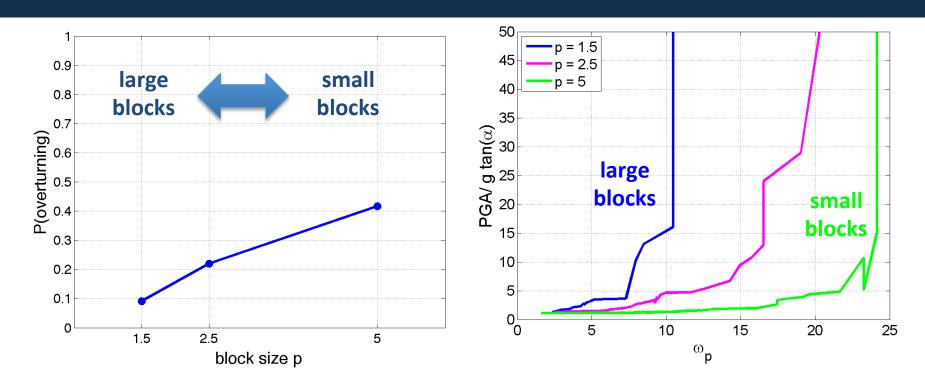




#### effect of the block slenderness $\lambda = h/b$ :

- $\lambda = h/b$  values considered: 2, 3, 5 and 10 ( $\alpha = 26.5, 18.4, 11.3, 5.7$ )
- slender blocks are susceptible to overturning since small PGAs can set them to rocking
- slender blocks topple for significantly smaller  $\alpha$ , therefore, they are more vulnerable to small-period ground motions (the threshold curves move towards larger  $\omega_{\text{D}}/\text{p}$  as  $\lambda$  increases).

## frequency parameter



#### effect of the frequency parameter $p = (3g/4R)^{0.5}$ :

- p values considered: 1.5, 2.5 and 5 (R = 3.3, 1.18, 0.30)
- Scale effect large blocks are more susceptible
- Small blocks overturn even for high-frequency records for which the large blocks are safe

Thank you for your attention